

*vibromachine,  
volumetric vibration treatment*

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## **INTENSIFICATION OF PROCESSES OF STRENGTHENING MACHINE PARTS BY VOLUMETRIC VIBRATION TREATMENT**

In order to calculate designed parameters for vibration machine of volumetric vibration treatment with the purpose to increase its productivity, the technique for investigating its dynamics based on non-linear complex mathematical model of the "vibromachine – treating medium" – system is suggested in this paper. As an example models of the machine with two independently driven vibrational exciters and the treating medium of its container are described. The calculation of optimal parameters is also suggested.

## **INTENSYFIKACJA PROCESÓW WZMOCNIENIA CZĘŚCI MASZYN ZA POMOCĄ METODY OBJĘTOŚCIOWEJ OBRÓBKI WIBRACYJNEJ**

W artykule prezentowana jest technika badania dynamiki maszyny wibracyjnej, w oparciu o nieliniowy złożony model matematyczny systemu "wibromaszyna – medium robocze". Celem badania jest obliczenie parametrów projektowych maszyny o podwyższonej wydajności. Jako przykładowe modele opisane są maszyny z dwoma niezależnie napędzanymi generatorami wibracji oraz medium roboczym jego zasobnika. Sugerowane są również obliczenia optymalnych parametrów.

Widespread application of volumetric treatment calls for a new approach to calculating and designing vibromachines (unbalanced drives, elastic elements, container cases, and other dynamically loaded parts), investigation of the processes which take place in the loaded container of the vibromachine while it moves as well as the influence of its parameters upon the process of treating, creation of the methods of computer designing of machines in general, and therefore thorough mathematical description of dynamic processes which take place in vibromachines during their work. Dynamic processes which take place in such complicated systems were described mainly in linear formulation that usually unadequately describes real physical phenomena of the process. The necessities of practice call for prognostication of treatment results depending on the form of the parts treated, their structures, physico-mechanical properties kind of friable treating medium as well as vibromachine characteristics taking into account the non-linear forces which take place in the case of their interaction.

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Solution of such complex problems which take into account the influence of the drive upon dynamics of different kinds of the medium and the body treated enables us to prognosticate the intensity of interaction between them (process of removing metal layer or superficial deformation of the parts treated), to properly choose geometrical and kinematic parameters of the vibromachine, and finally to lower material – and energy inputs as well as to increase the intensity of the treatment of articles.

It is suggested to solve the problems of this type through the elaboration and investigation of complex non-linear mathematic models of the “vibromachine – treating medium” – system by means of creating interconnected models of the motion of working tool of machine and friable medium; and on the basis of this dynamic phenomena of the system should be investigated in order to determine the influence of machine parameters and the medium upon factors of intensity of article treatment. The models are derived with taking into account unification and adequacy. The former (unification) enables us to apply them for designing and operating many types of machines provided they are parameterized; and this leads to time and material inputs reduction. The latter, because of the complication of the dynamics of “vibromachine – treating medium” – system, is possible only when the models obtained are non-linear.

By an example of vibromachine with two independently driven unbalance vibrational exciters, the complex model of the vibromachine and its medium is shown below; graphic correlations between the amplitude (as the main factor of article treating intensity in vibromachine) of the oscillation of the container and parameters of the machine are obtained; the parameters which according to the chosen criterion provide the maximum intensity of treating are calculated.

Vibromachine with two independently driven unbalance vibrational exciters are of several peculiarities which advantage them over other vibromachines. These advantages are the following:

- a) generation of oscillations of various forms (because of the two unbalance vibrational exciters),
- b) the possibility of the separation of the articles from the treating medium by means of redistribution of the oscillation amplitude of the working container on its plane during the treatment of articles or at the completion of treatment process due to the two independently driven vibrational exciters,
- c) relative simplicity of their designs and relatively high reliability of their parts in operation,
- d) their universality for modelling: the model includes, for example, the values of the masses of both unbalanced masses arbitrarily placed in the vibromachine; taking zero – value for one of the unbalanced masses enables us to employ this model for single – balance vibromachines with the unbalanced mass arbitrary placed with respect to its working container. In its turn, by means of the model derived, this enables us to investigate dynamic processes in vibromachines of other types;
- e) the possibility of automation of the process of volumetric vibrotreatment using the software elaborated on the basis of adequate mathematical models obtained as well as using results of investigating dynamic processes in vibromachines.

For investigation, the diagram of volumetric treatment vibromachine with two independently driven vibrational exciters [1] is shown in Fig.1.

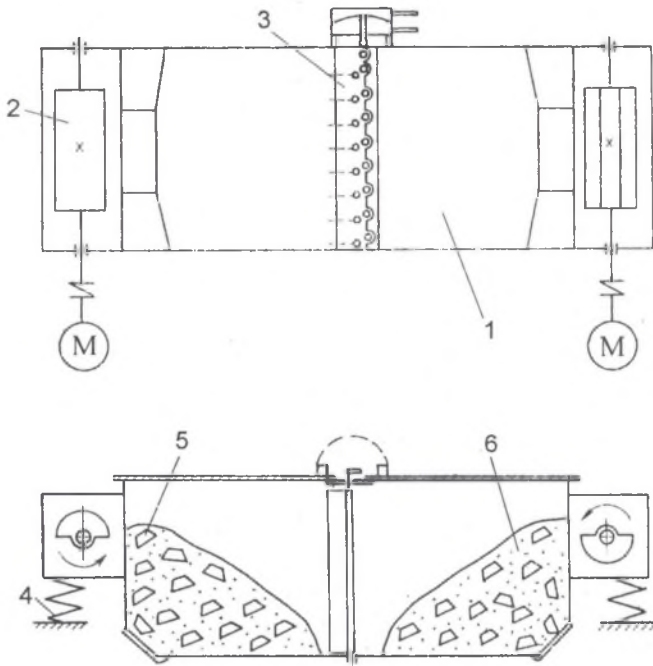


Fig.1. Unbalanced mass vibromachine with two independently driven vibrational exciters

The machine consists of container 1 with two unbalance vibrational exciters. The container is divided into two compartments by partition (jalousie) 3, and is mounted on elastic suspension 4. To the butt ends of the container two identical unbalance vibrational exciters are fastened 2. The unbalances are independently driven by corresponding electric motors through elastic muffs. The axes of rotating of the unbalances are parallel. There are treating medium 6 and treated articles 5 in both compartments of the container.

For the creation of the complex model of "vibromachine – treating medium" – system, separate models describing the motion of vibromachine container and the medium were driven, and finally they are united into the complex model of the system.

To derive the vibromachine container motion model, its diagram is drawn (Fig.2) where the vibromachine is depicted as plane mechanical system having several degrees of freedom, and the main geometric and kinematic parameters are given symbolically (parametrically) [2].

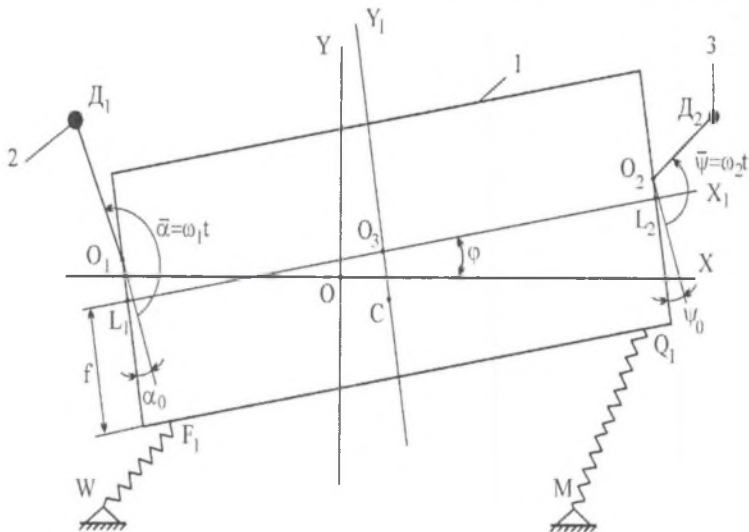


Fig.2. Diagram of generalized two-unbalance vibromachine

1 – working container; 2 – left unbalance ( $D_1$ ); 3 – right unbalance ( $D_2$ );  $XOY$  – fixed coordinate system;  $X_1O_3Y_1$  – moving coordinate system connected with geometric centre and symmetry axes of container;  $C$  – mass centre of container;  $f$  – distance between geometric centre and bottom of container;  $O_3L_1$  and  $O_3L_2$  – displacement of centers of rotation of unbalances with respect to vertical symmetre axis of container;  $WF_1$  and  $MQ_1$  – lengths of suspension springs at arbitrary instant of time during the motion of container.

Using Lagrange’s equations of II-nd type, the motion of the vibromachine container is described by means of the system of non-linear differential equations:

$$\begin{cases} \ddot{x}_c + \omega^2 x_c = \varepsilon f_x(\varphi, \dot{\varphi}, \ddot{\varphi}, \omega_1 t + \alpha_0, \omega_2 t + \psi_0) \\ \ddot{y}_c + \omega^2 y_c = \varepsilon f_y(\varphi, \dot{\varphi}, \ddot{\varphi}, \omega_1 t + \alpha_0, \omega_2 t + \psi_0) \\ \ddot{\varphi} + \omega_\varphi(t)\varphi = \varepsilon f_\varphi(\varphi, \dot{\varphi}, \ddot{\varphi}, \ddot{x}_c, \ddot{y}_c) \end{cases} \quad (1)$$

where  $x_c, y_c$  are coordinates of geometric centre of the container at arbitrary time instant  $t$ ;  $\varphi$  - angle of its turn;  $\omega$  - frequency of natural oscillations of the container;  $\varepsilon$  - small parameter;  $f_x, f_y, f_\varphi$  - functions which take into account physical and geometric non-linearity of mechanical system;  $\omega_\varphi(t)$  - frequency of circular oscillations of container, unbalances taken into account;  $\omega_i (i=1,2)$  - angular velocities of vibrational exciters motion,  $\omega_1 t + \alpha_0$  and  $\omega_2 t + \psi_0$  are their phases.

The first approximation of the solutions of system (1) is obtained by means of asymptotic methods of non-linear mechanics:

$$\left\{ \begin{array}{l} x_{o3} = x_0 \sin(\omega t + \alpha_x) + \frac{\varepsilon}{\omega} \int_0^t f_x(\varphi^*, \dot{\varphi}^*, \ddot{\varphi}^*, \omega_1 t + \alpha_0, \omega_2 t + \psi_0) \sin(\omega(t-u)) du \\ y_{o3} = y_0 \sin(\omega t + \alpha_y) + \frac{\varepsilon}{\omega} \int_0^t f_y(\varphi^*, \dot{\varphi}^*, \ddot{\varphi}^*, \omega_1 t + \alpha_0, \omega_2 t + \psi_0) \sin(\omega(t-u)) du \\ \varphi^* = \varphi_0 \cos(\omega_0 t + \theta(t)) \end{array} \right. \quad (2)$$

where  $\theta(t)$  is known function;  $\omega_0$ ,  $x_0$ ,  $y_0$ ,  $\alpha_x$  and  $\alpha_y$  are constants determined by parameters of the system and its initial condition.

An important stage in deriving models of such kind is the analysis of the stability of the solutions obtained in the form (2), i.e. the determination of the influence of parameters of this equation upon the character of its solution. Such analysis is necessary for ensuring perfect adequacy of the mathematical model to the real physical process both during designing and in the course of operating. It is necessary that the equation describing the model to have solution at intervals of time of any duration (the duration of treating articles in vibromachine may be considered unlimited). These laws of motion must meet the operational requirements of the system during the time interval of treating. As the result of investigation, it is found that for really existing parameters of the vibromachine the derived system of analytical expressions describes stable motion of the container.

The next stage of the work is the creation of the treating medium motion model of the vibromachine container [3,4]. For this purpose, the following hypotheses are assumed:

1. The material of the medium is continuous and homogeneous represented as stratification (multi-layer) of planar elastic-plastic beams, the thickness of which is considerably less than their length, and which in certain way contact with the container walls; in mathematical model this enables us to take into account both different kinds of interaction of working medium with the container and the motion of the container itself.
2. The medium moves layerwise and is in compound motion (in the plane of the motion of the container); the transportation motion of a layer is the motion (Fig.1) together with the vibromachine container, relative motion of a layer of the medium is the longitudinal oscillations along layer  $\xi$ . The schematic diagram of the compound motion of the cross-section of layer of the medium (point M of a volume element of the medium layer) is drawn in Fig.3. Such assumption enables us to mathematically describe the circulation of the medium in the container (volumewise) at different velocities.
3. The correlation between stress and deformation in the medium material is described by non-linear Föcht's law; the following two kinds of non-linearity are considered here:
  - a) non linearity of viscous stresses

$$\sigma = E\xi + k_0 \left( \frac{d\xi}{dt} \right)^{v+1} \quad (3)$$

- b) non linearity caused by elastic properties of the medium

$$\sigma = E(\zeta)^{\nu+1} + k_0 \frac{d\zeta}{dt} \tag{4}$$

where  $\sigma$  is normal stress in a layer of the medium;  $E$ ,  $k_0$ ,  $\nu$  are constants which characterize elastic and viscous properties of the medium;  $\zeta = \frac{\partial u}{\partial \xi}$  is its relative deformation (here  $u = u(\xi, t)$  is displacement of arbitrary cross – section of medium layer along axis  $\xi$  during a small interval of time  $t$ ).

4. In a layer of the medium as well as between layers, internal friction force is determined by means of Bolotin’s law:

$$R = \frac{\partial u}{\partial t} (B + B_0 u^2) \tag{5}$$

where  $B, B_0$  are constants determined by the kind of medium material.

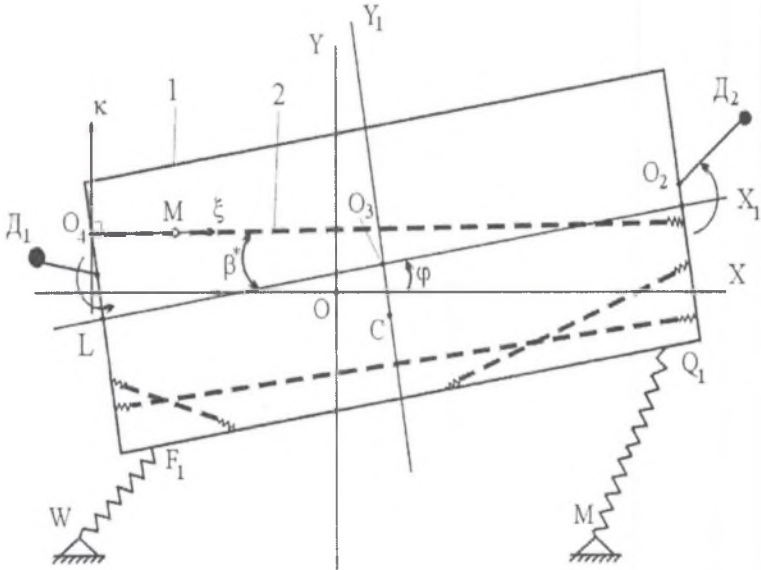


Fig.3. Graphic representation of vibromachine medium motion model

1–working container; 2– $i^{\text{th}}$  layer of the medium that represent elastic-plastic beam which elastically contacts the walls, of container;  $\xi O_4 \kappa$  – coordinate system bound with  $i^{\text{th}}$  layer of the medium;  $u(\xi, t)$  (point M) – arbitrary cross-section of  $i^{\text{th}}$  layer of the medium, in the relative motion this layer oscillates along axis  $\xi$ ;  $\beta^*$  – angle between coordinate system  $\xi O_4 \kappa$  and moving coordinate system  $Y_1 O_3 X_1$  which is bound with the geometric centre of the container (angle of inclination of  $i^{\text{th}}$  layer of the medium to the bottom of the container).

Under the assumptions mentioned, the equation of longitudinal oscillations (equation of relative motion of cross-section) of the medium layer takes the following forms:

a) form (3) in the case on non-linear Föcht's law

$$\frac{\partial^2 u}{\partial t^2} - \alpha^2 \frac{\partial^2 u}{\partial \xi^2} - \beta \left( \frac{\partial^3 u}{\partial \xi^2 \partial t} \right)^{\nu+1} = f(t) + \frac{\partial u}{\partial t} (\vartheta + \delta u^2) \tag{6}$$

b) form (4) in the case of nonlinear-elastic properties of friable medium

$$\frac{\partial^2 u}{\partial t^2} - \alpha^2 \frac{\partial}{\partial \xi} \left( \frac{\partial u}{\partial \xi} \right)^{\nu+1} - \beta \frac{\partial^3 u}{\partial \xi^2 \partial t} = f(t) + \frac{\partial u}{\partial t} (\vartheta + \delta u^2) \tag{7}$$

where  $\alpha, \beta, \vartheta, \delta$  are coefficients determined by the kind of medium material (metal balls, abrasive, etc.);  $f(t)$  is external disturbance caused by the motion of drive unbalanced masses.

It is assumed that in equations (6) and (7) the forces of viscous friction are small in comparison with non-linear-elastic (restoring) force in this layer, i.e.  $\beta, \vartheta, \delta \ll \alpha^2$ .

The model of medium layer motion with non-linear viscous component of stress is of the form:

$$\frac{\partial^2 u}{\partial t^2} - \alpha^2 \frac{\partial^2 u}{\partial \xi^2} = \varepsilon \left[ \left( \frac{\partial^3 u}{\partial \xi^2 \partial t} \right)^{\nu+1} + (\vartheta_1 + \delta_1 u^2) \frac{\partial u}{\partial t} + b_1 \sin \mu t \right] \tag{8}$$

Where  $\varepsilon b_1$  and  $\mu$  are parameters expressing the influence of external disturbance on the medium motion.

Unifrequent dynamic processes in the medium the motion of which can be described by means of (8), provided the interaction between the medium and the vibromachine container corresponds to hinge model of the contact between the medium and the working container ( $u(0, t) = u(l, t) = 0$ ), is described by the formula:

$$u_k(\xi, t) = a(t) \Xi_k(\xi) \cos(\omega_k^* t + \theta(t)) \tag{9}$$

where  $\omega_k^* = \alpha \frac{k\pi}{l}$  (here  $l$  is geometric parameter of container);  $k = 1, 2, \dots$

For the boundary conditions of nonlinear-elastic contact between the medium and the container:

$$\begin{aligned} \left[ \alpha_1 \frac{\partial u}{\partial \xi} + \beta_1 u \right]_{\xi=0} &= \varepsilon \varphi_1(\xi, t) \Big|_{\xi=0} \\ \left[ \alpha_2 \frac{\partial u}{\partial \xi} + \beta_2 u \right]_{\xi=l} &= \varepsilon \varphi_2(\xi, t) \Big|_{\xi=l} \end{aligned} \tag{10}$$

where  $\alpha_1, \alpha_2, \beta_1, \beta_2 \in [0, 1]$  are constants;  $\varphi_1(\xi, t) = h_1 u + d_1 u^3 - b_1 \sin \mu t$ ,  $\varphi_1(\xi, t) = -\varphi_2(\xi, t)$ , and  $h_1, d_1, h_2, d_2$  are parameters of nonlinear-elastic contact between the medium and the container, for the case of non-resonance we have:

$$u(\xi, t) = a_2 \Xi(\xi) \cos(\alpha \lambda_1 + \mu) t$$

where  $a_2 = \sqrt{\frac{\epsilon P_2}{2\alpha \lambda_1 \pi P_1 P_3}}$ ,  $P_3 = \delta_1 (\alpha \lambda_1 + \mu) \int_0^1 \Xi^4(\xi) d\xi$   
 $P_2 = \pi (\alpha \lambda_1 + \mu) \int_0^1 \Xi(\xi) \Xi''(\xi) d\xi + \vartheta_1 P_1$ ,  $P_1 = \int_0^1 \Xi^2(\xi) d\xi$ ,  $\Xi(\xi) = \sin \lambda_1 \xi - \frac{\alpha_1}{\beta_1} \lambda_1 \cos \lambda_1 \xi$ , and  $\lambda_1$  is the first eigen value of the boundary problem corresponding to non-disturbed motion equations (8), (10).

The model of medium layer motion with non-linear stress component is of the form

$$\frac{\partial^2 u}{\partial t^2} - \alpha^2 \frac{\partial}{\partial \xi} \left( \frac{\partial u}{\partial \xi} \right)^{\nu+1} = \epsilon \left[ b_1 \sin \mu t - (\vartheta_1 + \delta_1) \frac{\partial u}{\partial t} u^2 + \beta \frac{\partial^3 u}{\partial \xi^2 \partial t} \right] \tag{11}$$

The solutions of differential equations are obtained by means of special Atab-functions.

For stabilized mode of motion the equation of medium layer motion under the condition of rigid contact between the medium and container is of the form

$$u(\xi, t) = a(\nu) \text{sa} \left( 1, \frac{1}{\nu+1}, \Pi_\xi \frac{\xi}{l} \right) \text{ca}(\nu+1, l, \psi) \tag{12}$$

where

$$a(\nu) = \sqrt{\frac{\frac{8\pi \Gamma^2 \left( 1 + \frac{\nu}{2} \right) \Gamma^2 \left( \frac{1}{\nu+2} \right) - 4\vartheta_1 \sqrt{\pi} l \Gamma \left( \frac{1}{\nu+2} \right)}{(\nu+2)^2 l \Gamma^2 \left( \frac{3}{2} + \frac{1}{\nu+2} \right) (\nu+2) \Gamma \left( \frac{3}{2} + \frac{1}{\nu+2} \right)}}{\frac{3\delta_1 \pi \Gamma \left( \frac{3}{\nu+2} \right) \Gamma \left( \frac{\nu+1}{\nu+2} \right)}{8 \Gamma \left( \frac{3}{2} + \frac{3}{\nu+2} \right) \Gamma \left( \frac{5}{2} + \frac{\nu+1}{\nu+2} \right)} \cdot \frac{1}{\Pi_\xi}}$$

$\Pi_\xi = \sqrt{\pi} \Gamma \left( \frac{\nu+1}{\nu+2} \right) \Gamma^{-1} \left( \frac{1}{2} + \frac{\nu+1}{\nu+2} \right)$ ;  $\Gamma(\dots)$  is  $\gamma$  - function of corresponding argument.

Finally, the complex model of “vibromachine-treating medium”-system takes the form [5]:

$$\begin{cases} x_M(t) = x_{03}(t) + S \sin \varphi(t) - w \cos \varphi(t) - q \sin \varphi(t) + (\xi + u(\xi, t)) \cos(\varphi(t) + \beta^*) \\ y_M(t) = y_{03}(t) - S \cos \varphi(t) - w \sin \varphi(t) + q \cos \varphi(t) + (\xi + u(\xi, t)) \sin(\varphi(t) + \beta^*) \end{cases} \tag{13}$$

where  $S = O_3C$  is the distance between geometric centre of the container and the mass centre of the medium,  $\xi = O_4M$ , is a position of an element of medium layer at initial instant of time,  $u(\xi, t)$  is the law of longitudinal oscillations of the layer (law of relative motion), which is described by corresponding equations for a resonance case of medium motion or non-resonance one,  $w = LO_3$ ,  $q = LO_4$ .

By means of the complex model obtained it is possible to investigate different modes of the motion of the vibromachine and the medium, to plot trajectories of motion for arbitrary points of the container and the medium, to investigate the influence of the parameters of the



vibromachine and the medium on the factors of the intensity of articles treatment according to corresponding criterion of intensity.

Graphic correlation's obtained by means of the complex model and the software elaborated on its basis are shown in Fig.4; they illustrate the influence of vibromachine parameters upon the amplitude of its container oscillations; the amplitude is the main factor of the articles treatment intensity according to such criterion of intensity as removing metal from the surface of the treated article per unit of time.

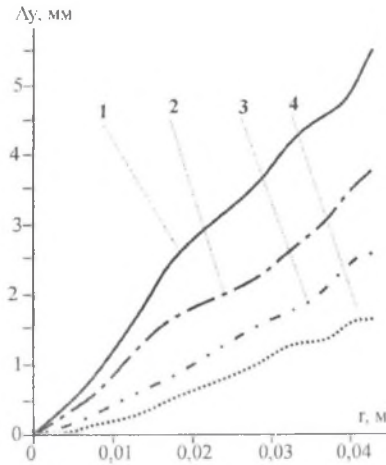


Fig.4. Correlation between vertical component of container oscillation and radius of unbalanced masses  
 1. mass of 9.238 kg; 2. mass of 6.927 kg; 3. mass of 4.618 kg; 4. mass of 2.309 kg

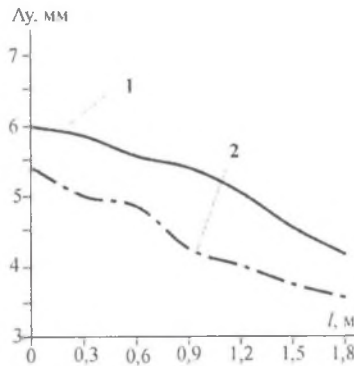


Fig.5. Correlation between amplitude of vibromachine container and the placement of suspension attachment  
 1. oscillating mass 70 kg; 2. oscillating mass 84 kg

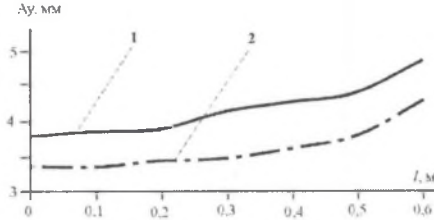


Fig. 6. Correlation between vibromachine container oscillations and the placement of unbalance units  
1. oscillating mass 70 kg; 2. oscillating mass 84 kg

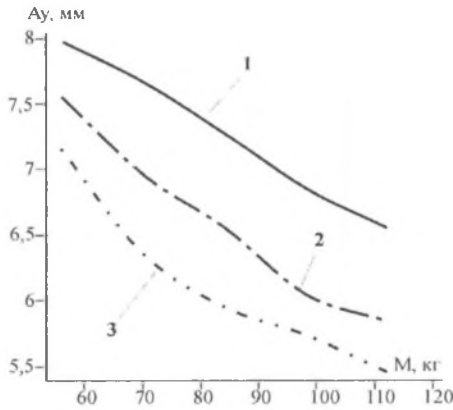


Fig. 7. Correlation between amplitude of vertical oscillation of container centre and oscillating mass at unbalance rotation angular velocity of  $w_2 = 96 \text{ s}^{-1}$   
1. rigidity of suspension (left or right) 22860 N/m; 2. rigidity of suspension (left or right) 34290 N/m;  
3. rigidity of suspension (left or right) 45710 N/m

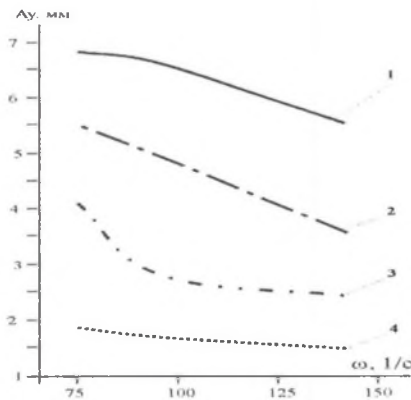


Fig. 8. Correlation between vertical component of container oscillation and angular velocity of rotation unbalanced mass  
1. mass of 9.238 kg; 2. mass of 6.927 kg; 3. mass of 4.618 kg; 4. mass of 2.309 kg

The chosen mechanical criterion of intensivity – “removing of material from the article surface per unit time” is proportional to the square of amplitude and to the cube of oscillation frequency of container [6,7]:

$$q = k \cdot a^2 \cdot \omega^3$$

where  $q$  (g/s) is amount of material removed per unit of time,  $a$  (mm) – amplitude of container oscillation,  $\omega$  ( $c^{-1}$ ) – container oscillation frequency,  $k$  (g/mm) – empirical constant taking into account the other parameters of vibrotreating (influence of vibromachine parameters of treading medium, etc. )

Finally, on the basis of investigations carried out, parameters and the mode of work of the two-unbalanced masses vibromachine (input data: mass of container – 55kg, its length 0.59m, distance between supports – 0.77m, frequency of vibration – 22.5Hz, mass of the load – 20kg in the form of metal balls 0.005m in diameter) which ensure the highest intensivity of article treatment (in this particular case-the largest removing of material from the article surface per unit of time) are the following:

- a) unbalanced masses of vibromachine should rotate in the same sense, that ensure the most intensive mixing and circulation of treating medium in working container volumewise;
- b) rigidity of working suspension (total) – 45720 N/m;
- c) angular velocity of unbalance rotation –  $141c^{-1}$ ;
- d) unbalanced mass – 9.238kg;
- e) radius of unbalanced mass – 0.0424m(static moment of unbalanced mass 0.3921kg·m);
- f) length of vibromachine container – 0.5m;
- g) distance between attachment of unbalance units and container bottom – 0.6m.

Thus, the obtained complex mathematical model of “vibromachine – trading medium” – system enables us to analytically determine the influence of its parameters upon the intensivity of articles treatment in it according to the chosen criterion; thus it saves us from carrying out time taking cumbersome experiments both for designing a vibromachine and for selecting modes of treating articles in it. Due to their non-linearity, models of such kind are adequate to real situation of vibrotreatment, they can also be applied in investigation of dynamics of the vibromachine and its medium.

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